

Machine-Level Prog. IV - Structured Data



Today

- Arrays
- Structures
- Unions

Next time

- Buffers

Basic data types

- Integral

- Stored & operated on in general registers
- Signed vs. unsigned depends on instructions used

Intel	GAS	Bytes	C
byte	b	1	[unsigned] char
word	w	2	[unsigned] short
double word	l	4	[unsigned] int

- Floating point

- Stored & operated on in floating point registers

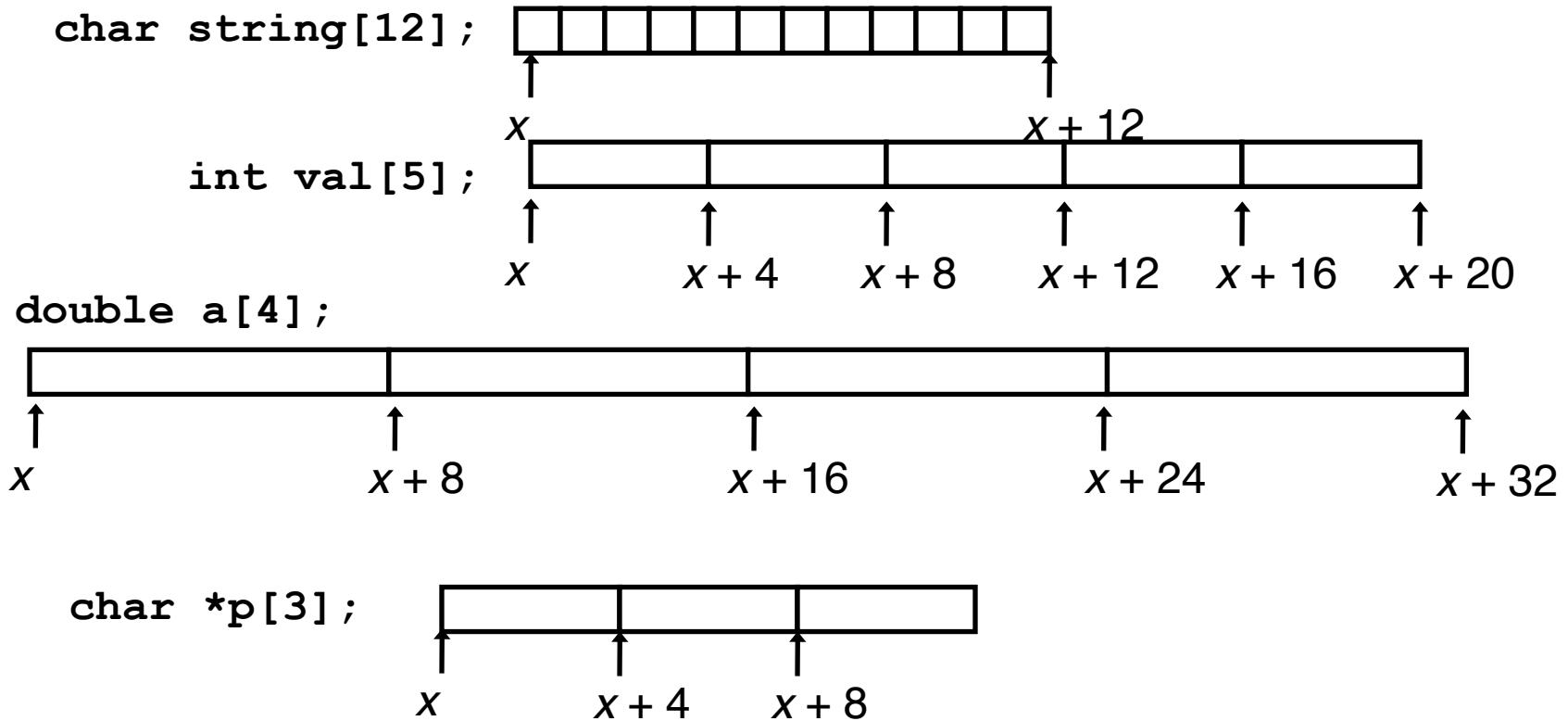
Intel	GAS	Bytes	C
Single	s	4	float
Double	l	8	double
Extended	t	10/12	long double

Array allocation

- Basic principle

$T A[L];$

- Array of data type T and length L
- Contiguously allocated region of $L * \text{sizeof}(T)$ bytes

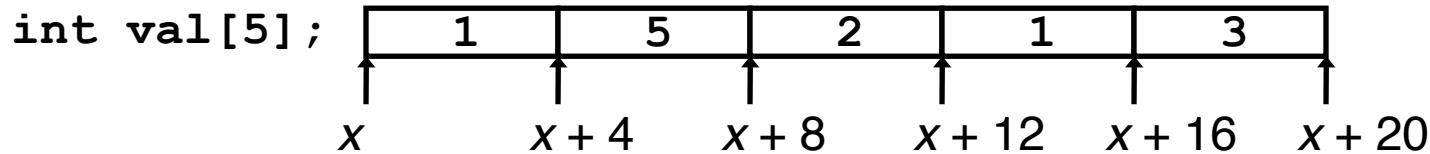


Array access

- Basic principle

$T \ A[L];$

- Identifier A can be used as a pointer to array element 0



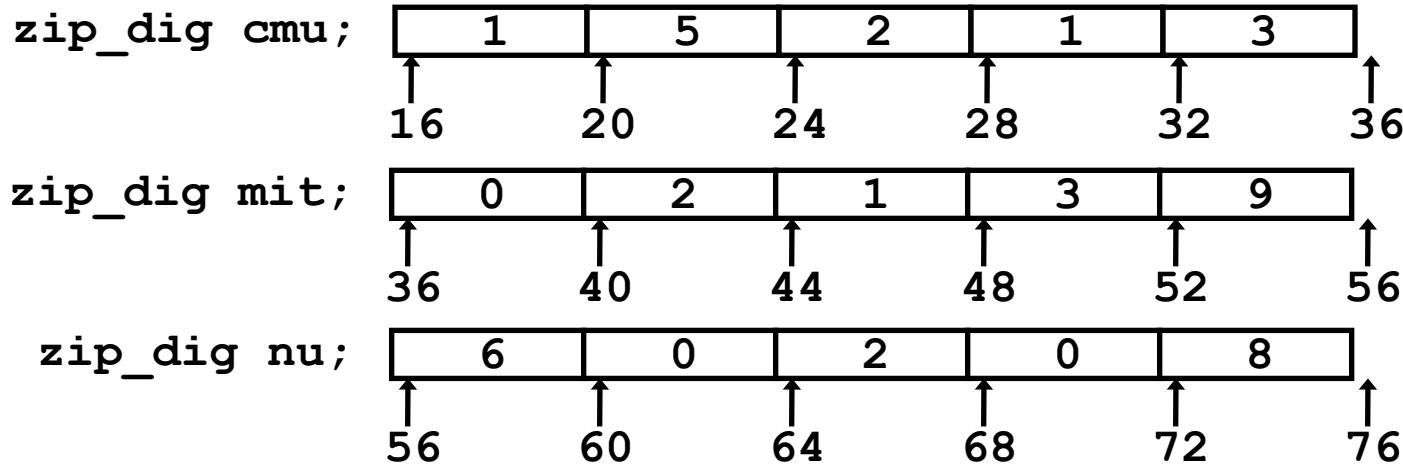
- Reference Type Value

<code>val[4]</code>	<code>int</code>	3
<code>val</code>	<code>int *</code>	x
<code>val+1</code>	<code>int *</code>	$x + 4$
<code>&val[2]</code>	<code>int *</code>	$x + 8$
<code>val[5]</code>	<code>int</code>	??
<code>* (val+1)</code>	<code>int</code>	5
<code>val + i</code>	<code>int *</code>	$x + 4 \ i$

Array example

```
typedef int zip_dig[5];

zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig nu = { 6, 0, 2, 0, 8 };
```



Notes

- Declaration “`zip_dig nu`” equivalent to “`int nu[5]`”
- Example arrays were allocated in successive 20 byte blocks
 - Not guaranteed to happen in general

Array accessing example

- Computation

- Register `%edx` contains starting address of array
- Register `%eax` contains array index
- Desired digit at $4 * \%eax + \%edx$
- Use memory reference (`%edx`,
`%eax`, 4)

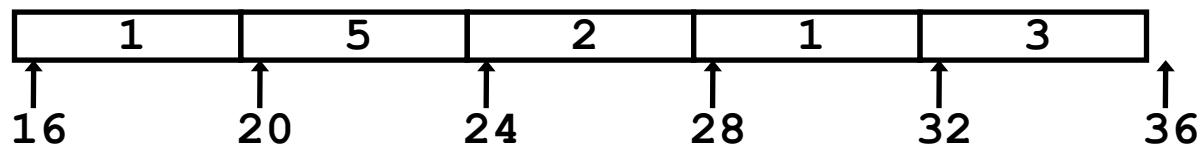
```
int get_digit
    (zip_dig z, int dig)
{
    return z[dig];
}
```

Memory reference code

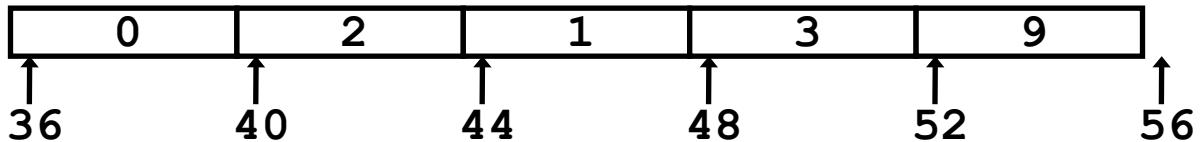
```
# %edx = z
# %eax = dig
movl (%edx,%eax,4),%eax # z[dig]
```

Referencing examples

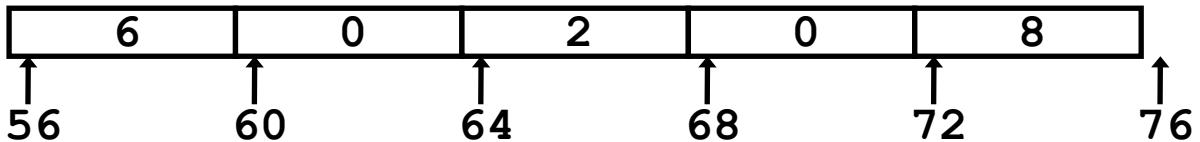
`zip_dig cmu;`



`zip_dig mit;`



`zip_dig nu;`



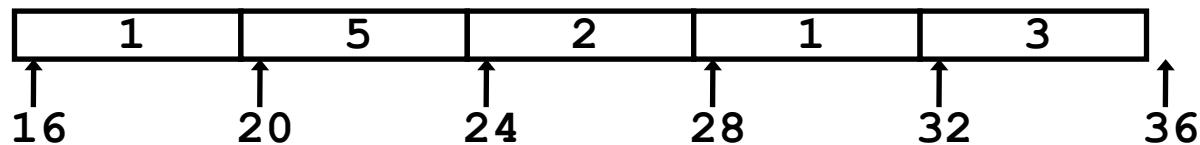
- Code does not do any bounds checking!

Reference	Address	Value	Guaranteed?
mit[3]	$36 + 4 * 3 = 48$	3	
mit[5]	$36 + 4 * 5 = 56$	6	
mit[-1]	$36 + 4 * -1 = 32$	3	
cmu[15]	$16 + 4 * 15 = 76$??	

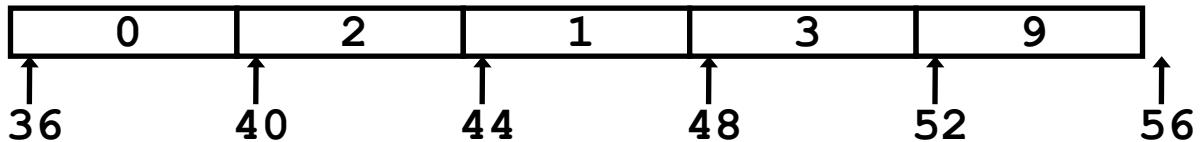
- Out of range behavior implementation-dependent
 - No guaranteed relative allocation of different arrays

Referencing examples

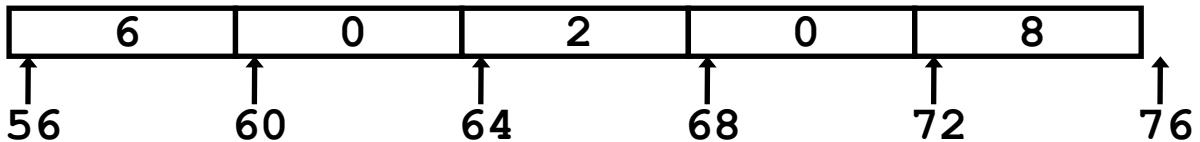
`zip_dig cmu;`



`zip_dig mit;`



`zip_dig nu;`



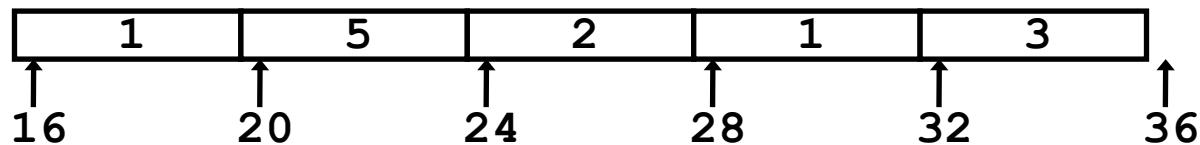
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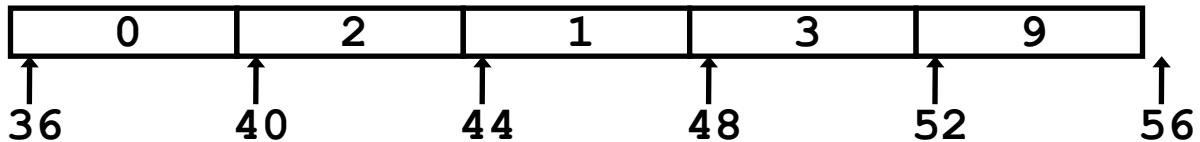
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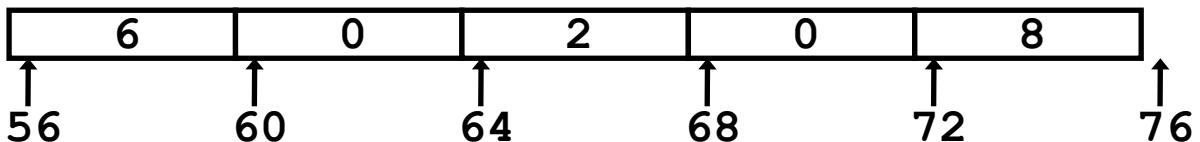
`zip_dig cmu;`



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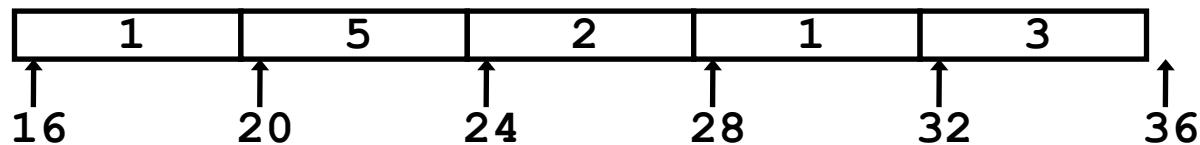
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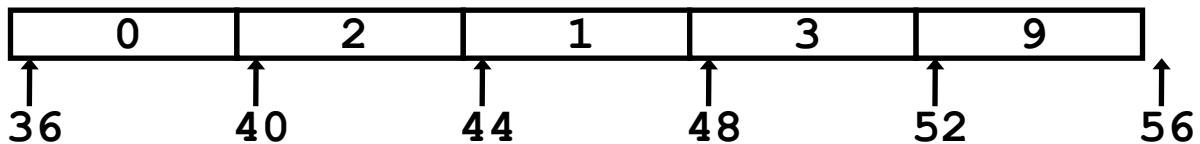
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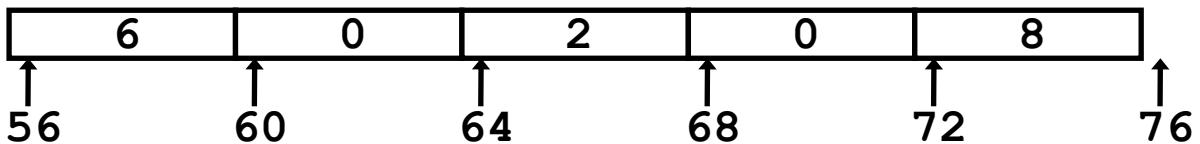
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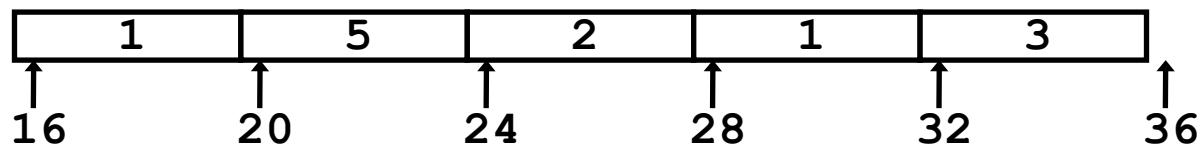
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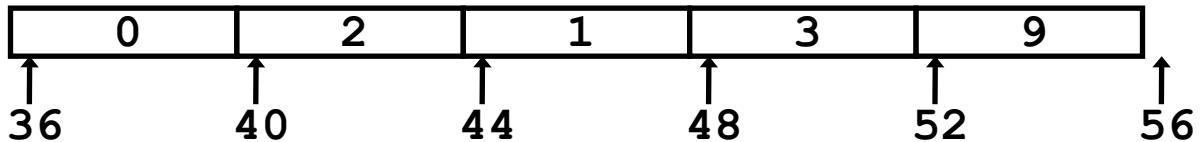
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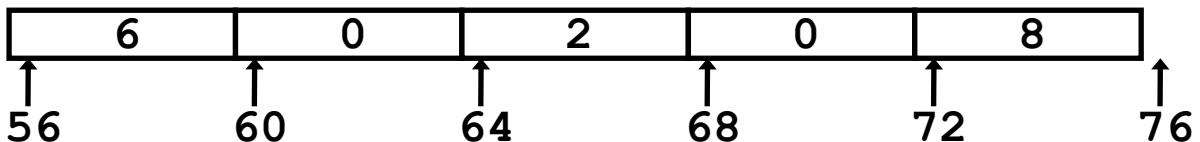
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- Out of range behavior implementation-dependent
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Array loop example

- Original Source

Computes the integer represented by an array of 5 decimal digits.

```
int zd2int(zip_dig z)
{
    int i;
    int zi = 0;
    for (i = 0; i < 5; i++) {
        zi = 10 * zi + z[i];
    }
    return zi;
}
```

- Transformed version

As generated by GCC

- Eliminate loop variable `i` and uses pointer arithmetic
- Computes address of final element and uses that for test
- Express in do-while form
 - No need to test at entrance

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
    do {
        zi = 10 * zi + *z;
        z++;
    } while(z <= zend);
    return zi;
}
```

Array loop implementation

- Registers

- %ecx z
- %eax zi
- %ebx zend

- Computations

- $10 * zi + *z$ implemented as
 $*z + 2 * (zi + 4 * zi)$
- $z++$ increments by 4

```
int zd2int(zip_dig z)
{
    int zi = 0;
    int *zend = z + 4;
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        zi = 10 * zi + *z;
        z++;
    } while(z <= zend);
    return zi;
}
```

```
# %ecx = z
xorl %eax,%eax          # zi = 0
leal 16(%ecx),%ebx       # zend = z+4
.L59:
    leal (%eax,%eax,4),%edx      # 5*zi
    movl (%ecx),%eax            # *z
    addl $4,%ecx               # z++
    leal (%eax,%edx,2),%eax      # zi = *z + 2*(5*zi)
    cmpl %ebx,%ecx             # z : zend
    jle .L59                   # if <= goto loop
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Checkpoint

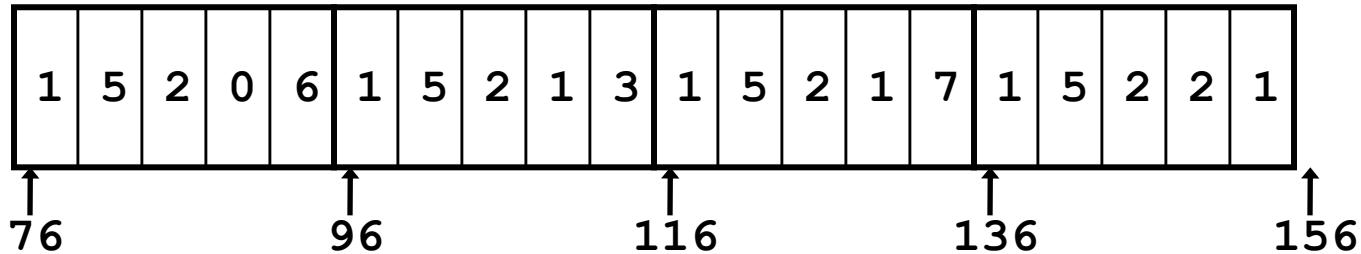
Checkpoint



Nested array example

```
#define PCOUNT 4
zip_dig pgm[PCOUNT] =
    {{1, 5, 2, 0, 6},
     {1, 5, 2, 1, 3 },
     {1, 5, 2, 1, 7 },
     {1, 5, 2, 2, 1 }};
```

zip_dig
pgm[4];



- Declaration “zip_dig pgm[4]” equivalent to “int pgm[4][5]”
 - Variable pgm denotes array of 4 elements
 - Allocated contiguously
 - Each element is an array of 5 int’s

Nested array allocation

- Declaration

$T A[R][C];$

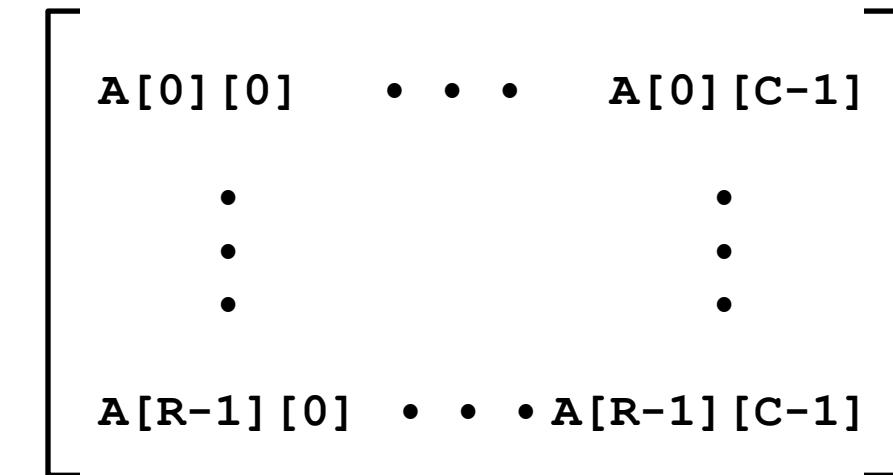
- Array of data type T
- R rows, C columns
- Type T element requires K bytes

- Array size

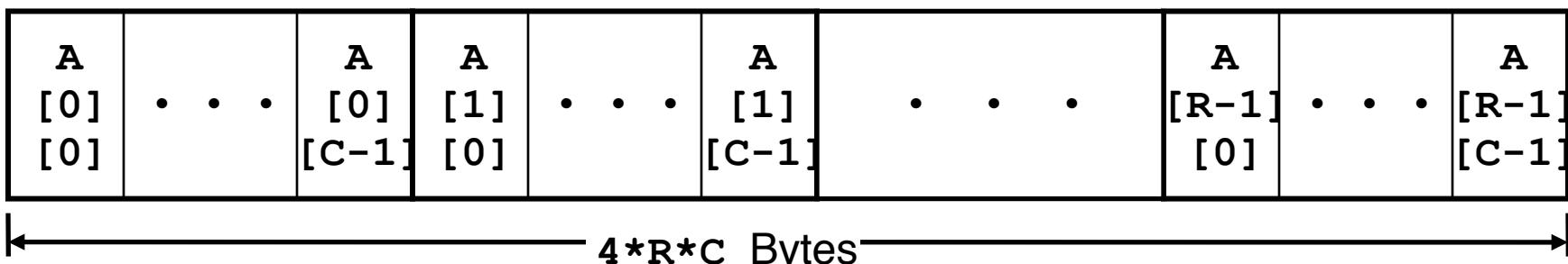
- $R * C * K$ bytes

- Arrangement

- Row-Major Ordering



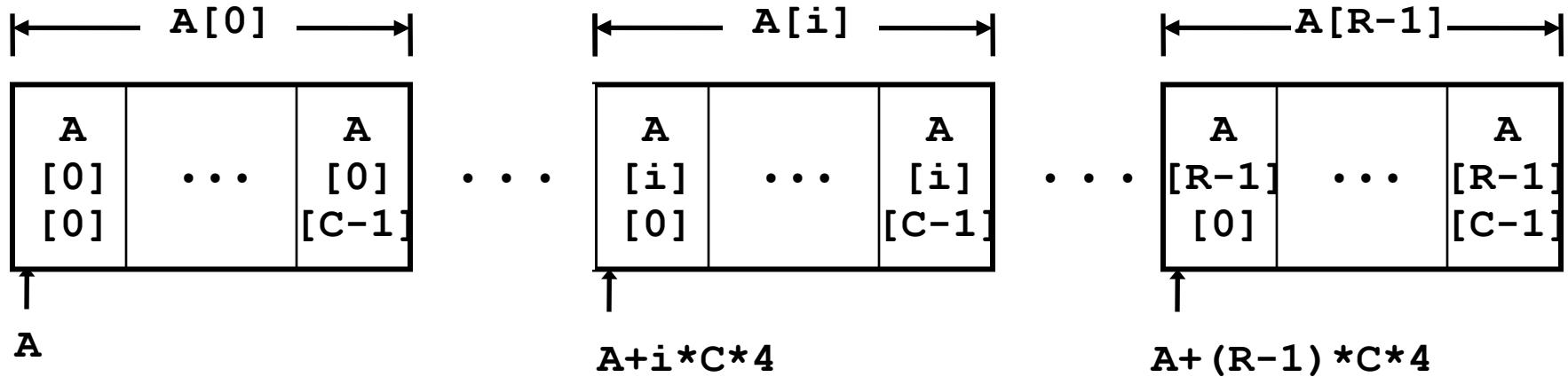
`int A[R][C];`



Nested array row access

- Row vectors
 - $A[i]$ is array of C elements
 - Each element of type T
 - Starting address $A + i * C * K$ ($\text{sizeof}(T) = K$)

```
int A[R][C];
```



Nested array row access code

```
int *get_pgh_zip(int index)
{
    return pgh[index];
}
```

- Row vector
 - `pgh[index]` is array of 5 int's
 - Starting address `pgh+20*index`
- Code
 - Computes and returns address
 - Compute as `pgh + 4*(index+4*index)`

```
# %eax = index
leal (%eax,%eax,4),%eax # 5 * index
leal pgh(%eax,4),%eax # pgh + (20 * index)
```

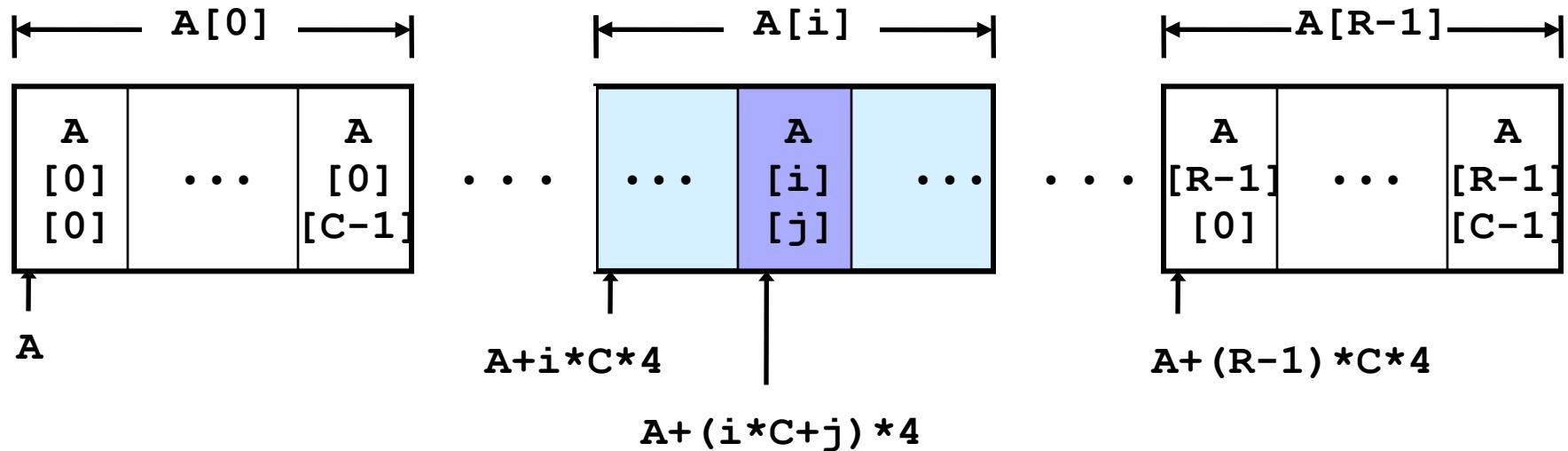
Nested array element access

- Array elements

- $A[i][j]$ is element of type T
- Address $A + (i * C + j) * K$



```
int A[R][C];
```



Nested array element access code

- Array Elements

- `pgh[index][dig]` is int
- Address:
$$\text{pgh} + 4 * (5 * \text{index} + \text{dig}) =$$

$$\text{pgh} + 20 * \text{index} + 4 * \text{dig}$$

```
int get_pgh_digit
    (int index, int dig)
{
    return pgh[index][dig];
}
```

- Code

- Computes address

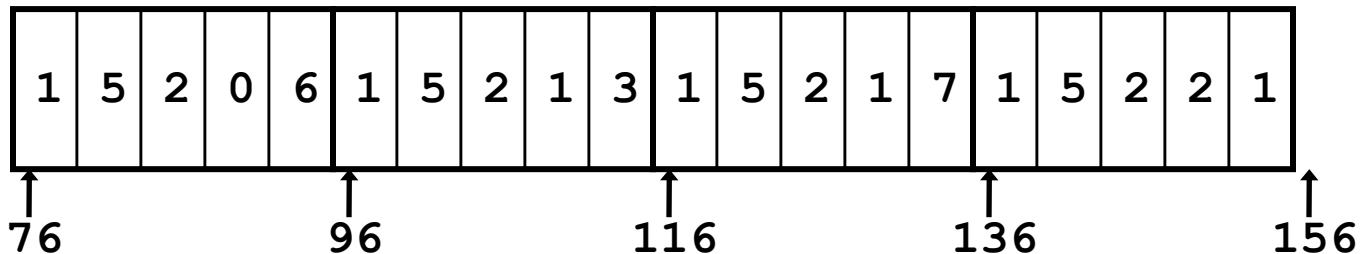
$$\text{pgh} + 4 * \text{dig} + 4 * (\text{index} + 4 * \text{index})$$

- `movl` performs memory reference

```
# %ecx = dig
# %eax = index
leal 0(%ecx,4),%edx          # 4*dig
leal (%eax,%eax,4),%eax      # 5*index
movl pgh(%edx,%eax,4),%eax   # * (pgh + 4*dig + 20*index)
```

Strange referencing examples

`zip_dig`
`pgh[4];`



Reference	Address	Value Guaranteed?
-----------	---------	-------------------

`pgh[3][3]` $76+20*3+4*3 = 148$ 2

`pgh[2][5]` $76+20*2+4*5 = 136$ 1

`pgh[2][-1]` $76+20*2+4*-1 = 112$ 3

`pgh[4][-1]` $76+20*4+4*-1 = 152$ 1

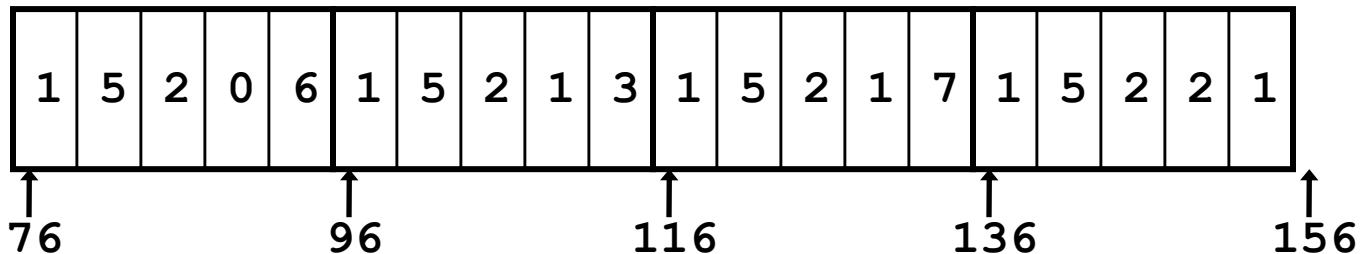
`pgh[0][19]` $76+20*0+4*19 = 152$ 1

`pgh[0][-1]` $76+20*0+4*-1 = 72$??

- Code does not do any bounds checking
- Ordering of elements within array guaranteed

Strange referencing examples

`zip_dig`
`pgh[4];`



Reference	Address	Value Guaranteed?
<code>pgh[3][3]</code>	$76 + 20 * 3 + 4 * 3 = 148$	2
<code>pgh[2][5]</code>	$76 + 20 * 2 + 4 * 5 = 136$	1
<code>pgh[2][-1]</code>	$76 + 20 * 2 + 4 * -1 = 112$	3
<code>pgh[4][-1]</code>	$76 + 20 * 4 + 4 * -1 = 152$	1
<code>pgh[0][19]</code>	$76 + 20 * 0 + 4 * 19 = 152$	1
<code>pgh[0][-1]</code>	$76 + 20 * 0 + 4 * -1 = 72$??

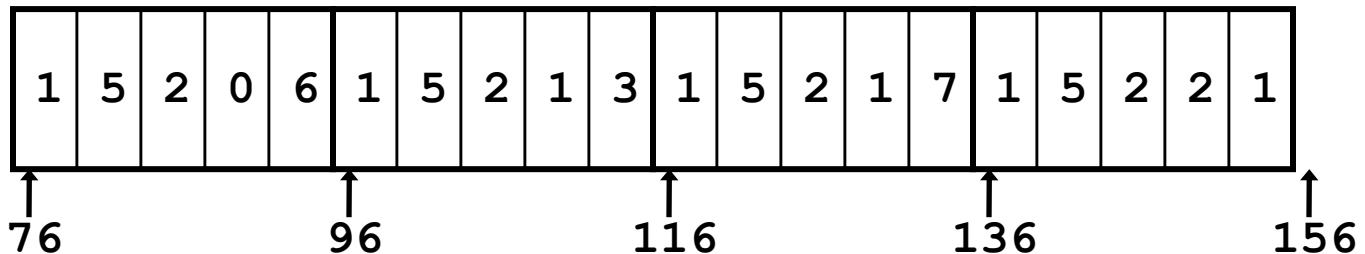
Yes

- Code does not do any bounds checking

- Ordering of elements within array guaranteed

Strange referencing examples

`zip_dig`
`pgh[4];`

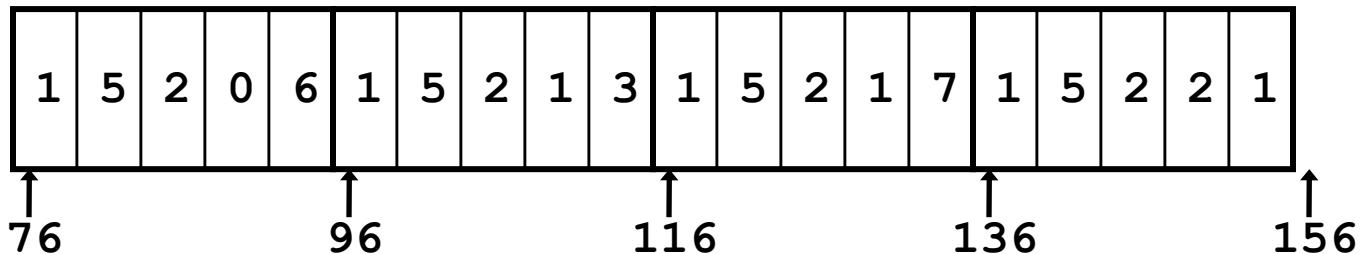


Reference	Address	Value Guaranteed?
<code>pgh[3][3]</code>	$76 + 20 * 3 + 4 * 3 = 148$	2 Yes
<code>pgh[2][5]</code>	$76 + 20 * 2 + 4 * 5 = 136$	1 Yes
<code>pgh[2][-1]</code>	$76 + 20 * 2 + 4 * -1 = 112$	3
<code>pgh[4][-1]</code>	$76 + 20 * 4 + 4 * -1 = 152$	1
<code>pgh[0][19]</code>	$76 + 20 * 0 + 4 * 19 = 152$	1
<code>pgh[0][-1]</code>	$76 + 20 * 0 + 4 * -1 = 72$??

– Code does not do any bounds checking
– Ordering of elements within array guaranteed

Strange referencing examples

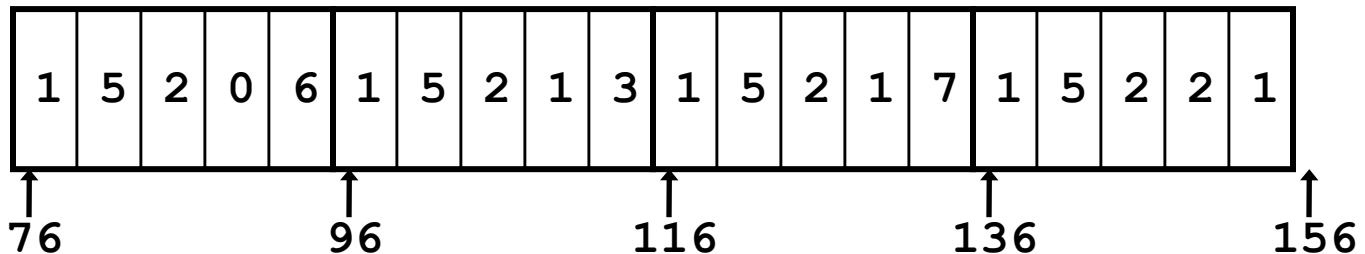
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Strange referencing examples

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`pgh[4];`

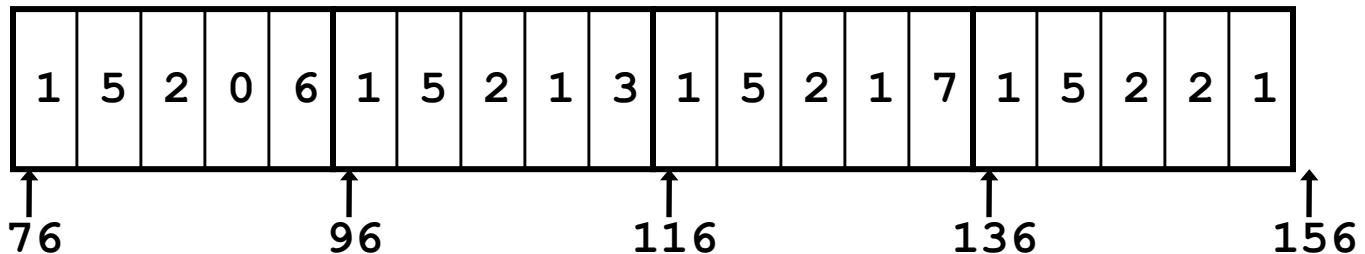


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Strange referencing examples

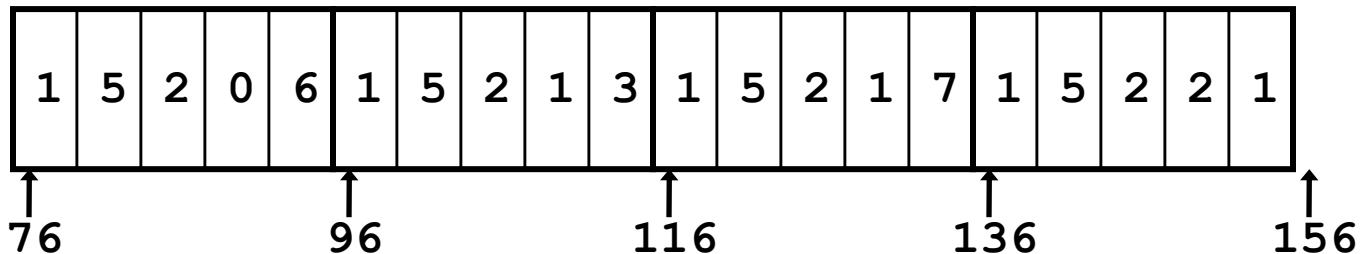
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Strange referencing examples

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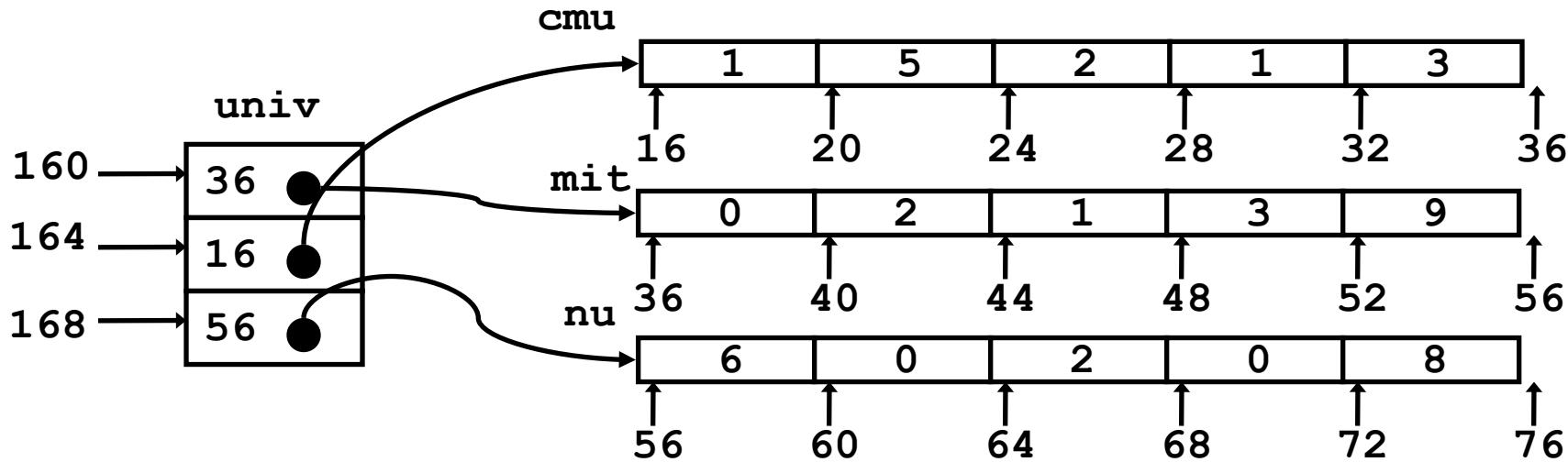
– Code does not do any bounds checking
– Ordering of elements within array guaranteed

Multi-level array example

- Variable `univ` denotes array of 3 elements
- Each element is a pointer
 - 4 bytes
- Each pointer points to array of `int`'s

```
zip_dig cmu = { 1, 5, 2, 1, 3 };
zip_dig mit = { 0, 2, 1, 3, 9 };
zip_dig nu = { 6, 0, 2, 0, 8 };
```

```
#define UCOUNT 3
int *univ[UCOUNT] = {mit, cmu, nu};
```



Element access in multi-level array

```
int get_univ_digit  
    (int index, int dig)  
{  
    return univ[index][dig];  
}
```

- Computation

- Element access $\text{Mem}[\text{Mem}[\text{univ} + 4 * \text{index}] + 4 * \text{dig}]$
- Must do two memory reads
 - First get pointer to row array
 - Then access element within array

```
# %ecx = index  
# %eax = dig  
leal 0(%ecx, 4), %edx      # 4*index  
movl univ(%edx), %edx      # Mem[univ+4*index]  
movl (%edx, %eax, 4), %eax # Mem[...+4*dig]
```

Array element accesses

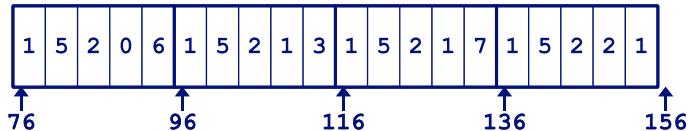
Similar C references

- Nested Array

```
int get_pgh_digit
    (int index, int dig)
{
    return pgh[index][dig];
}
```

- Element at

Mem[pgh+20*index+
4*dig]



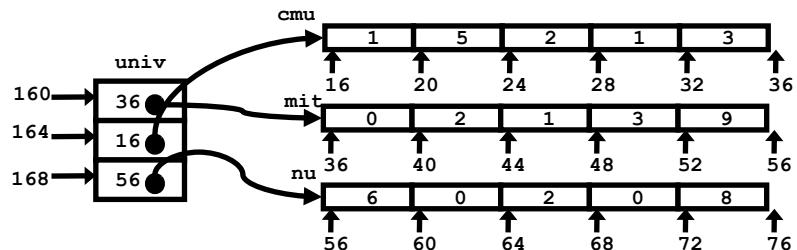
Different address computation

- Multi-Level Array

```
int get_univ_digit
    (int index, int dig)
{
    return univ[index][dig];
}
```

- Element at

Mem[Mem[univ+4*index]
+4*dig]



Using nested arrays

- Strengths

- C compiler handles doubly subscripted arrays
- Generates very efficient code
 - Avoids multiply in index computation

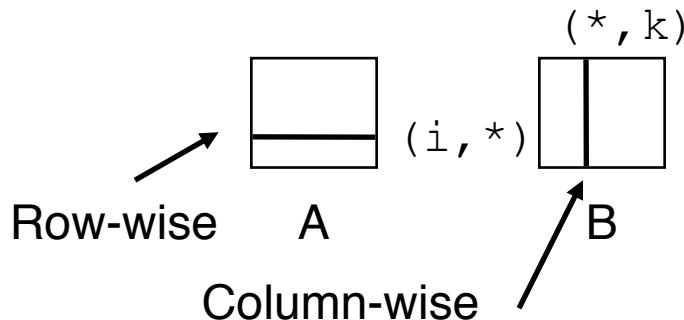
- Limitation

- Only works if have fixed array size

```
#define N 16
typedef int fix_matrix[N][N];
```

```
/* Compute element i,k of
   fixed matrix product */
int fix_prod_ele(fix_matrix a,
                  fix_matrix b,
                  int i, int k)
{
    int j;
    int result = 0;
    for (j = 0; j < N; j++)
        result += a[i][j]*b[j][k];

    return result;
}
```



Dynamic nested arrays

- Strength
 - Can create matrix of arbitrary size
- Programming
 - Must do index computation explicitly
- Performance
 - Accessing single element costly
 - Must do multiplication

```
int *new_var_matrix(int n)
{
    return (int *)
        calloc(sizeof(int), n*n);
}
```

```
int var_ele (int *a, int i,
             int j, int n)
{
    return a[i*n+j];
}
```

```
movl 12(%ebp),%eax          # i
movl 8(%ebp),%edx           # a
imull 20(%ebp),%eax         # n*i
addl 16(%ebp),%eax          # n*ii+j
movl (%edx,%eax,4),%eax     # Mem[a+4*(i*n+j)]
```

Dynamic array multiplication

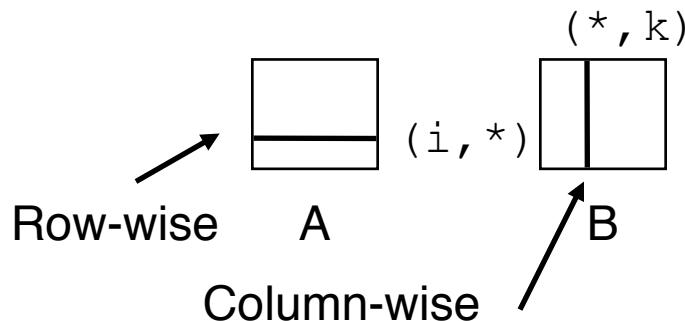
- Without optimizations

- Multiplies

- 2 for subscripts
 - 1 for data

- Adds

- 4 for array indexing
 - 1 for loop index
 - 1 for data



```
/* Compute element i,k of
   variable matrix product */
int var_prod_ele (int *a, int *b,
                   int i, int k,
                   int n)
{
    int j;
    int result = 0;
    for (j = 0; j < n; j++)
        result +=
            a[i*n+j] * b[j*n+k];

    return result;
}
```

Optimizing dynamic array mult.

- Optimizations
 - Performed when set
 - optimization level to -O2
- Code motion
 - Expression $i * n$ can be computed outside loop
- Strength reduction
 - Incrementing j has effect of incrementing $j * n + k$ by n
- Performance
 - Compiler can optimize regular access patterns

```
{  
    int j;  
    int result = 0;  
    for (j = 0; j < n; j++)  
        result +=  
            a[i*n+j] * b[j*n+k];  
    return result;  
}
```

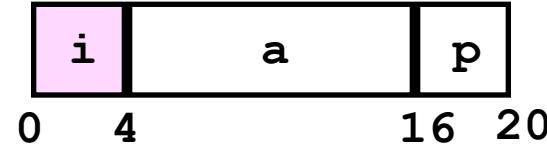
```
{  
    int j;  
    int result = 0;  
    int iTn = i*n;  
    int jTnPk = k;  
    for (j = 0; j < n; j++) {  
        result +=  
            a[iTn+j] * b[jTnPk];  
        jTnPk += n;  
    }  
    return result;  
}
```

Structures

- Concept
 - Members may be of different types
 - Contiguously-allocated region of memory
 - Refer to members within structure by names

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```

Memory Layout



- Accessing structure member

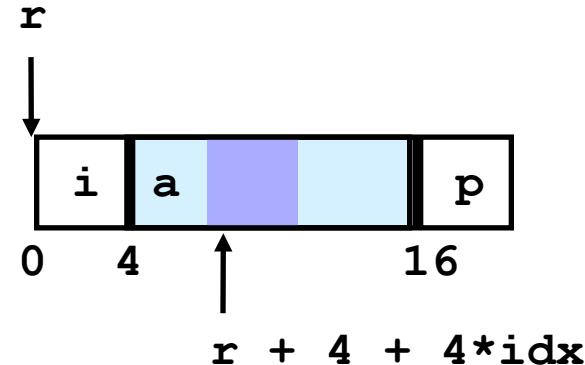
```
void  
set_i(struct rec *r, int val)  
{  
    r->i = val;  
}
```

Assembly

```
# %eax = val  
# %edx = r  
movl %eax, (%edx) # Mem[r] = val
```

Generating pointer to struct. member

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```



- Generating Pointer to Array Element
 - Offset of each structure member determined at compile time

```
int *  
find_a  
(struct rec *r, int idx)  
{  
    return &r->a[idx];  
}
```

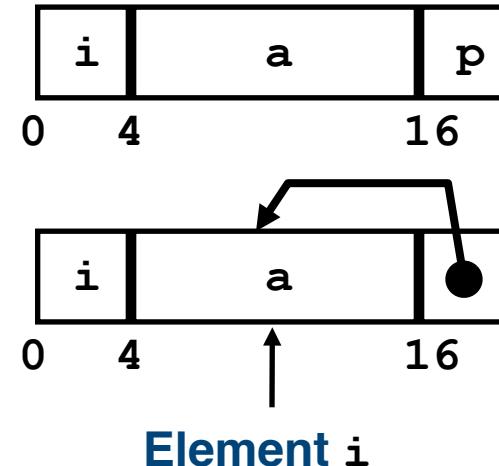
```
# %ecx = idx  
# %edx = r  
leal 0(%ecx,4),%eax    # 4*idx  
leal 4(%eax,%edx),%eax # r+4*idx+4
```

Structure referencing (Cont.)

- C Code

```
struct rec {  
    int i;  
    int a[3];  
    int *p;  
};
```

```
void  
set_p(struct rec *r)  
{  
    r->p =  
        &r->a[r->i];  
}
```



Element i

```
# %edx = r  
movl (%edx),%ecx          # r->i  
leal 0(%ecx,4),%eax       # 4*(r->i)  
leal 4(%edx,%eax),%eax   # r+4+4*(r->i)  
movl %eax,16(%edx)        # Update r->p
```

Checkpoint

Checkpoint



Alignment

- Aligned data
 - Primitive data type requires K bytes
 - Address must be multiple of K
 - Required on some machines; advised on IA32
 - treated differently by Linux and Windows!
- Motivation for aligning data
 - Memory accessed by (aligned) double or quad-words
 - Inefficient to load or store datum that spans quad word boundaries
 - Virtual memory very tricky when datum spans 2 pages
- Compiler
 - Inserts gaps in structure to ensure correct alignment of fields

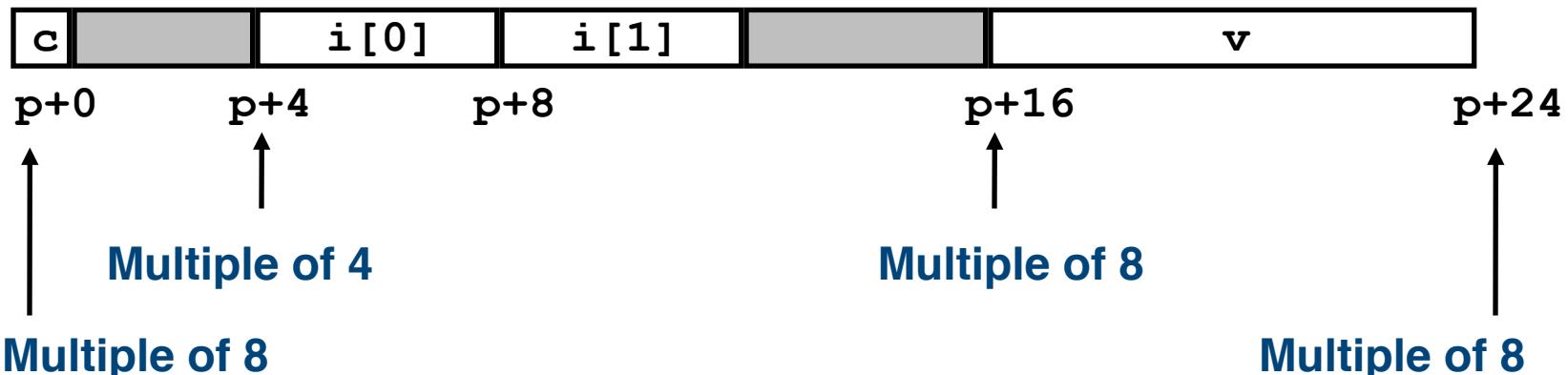
Specific cases of alignment

- Size of Primitive Data Type:
 - 1 byte (e.g., `char`)
 - no restrictions on address
 - 2 bytes (e.g., `short`)
 - lowest 1 bit of address must be 0_2
 - 4 bytes (e.g., `int`, `float`, `char *`, etc.)
 - lowest 2 bits of address must be 00_2
 - 8 bytes (e.g., `double`)
 - Windows (and most other OS's & instruction sets):
 - lowest 3 bits of address must be 000_2
 - Linux:
 - lowest 2 bits of address must be 00_2
 - i.e., treated the same as a 4-byte primitive data type
 - 12 bytes (`long double`) [only 10 bytes needed]
 - Linux and Windows:
 - lowest 2 bits of address must be 00_2
 - i.e., treated the same as a 4-byte primitive data type

Satisfying alignment with structures

- Offsets Within Structure
 - Must satisfy element's alignment requirement
- Overall Structure Placement
 - Each structure has alignment requirement K
 - Largest alignment of any element
 - Initial address & structure length must be multiples of K
- Example (under Windows):
 - K = 8, due to `double` element

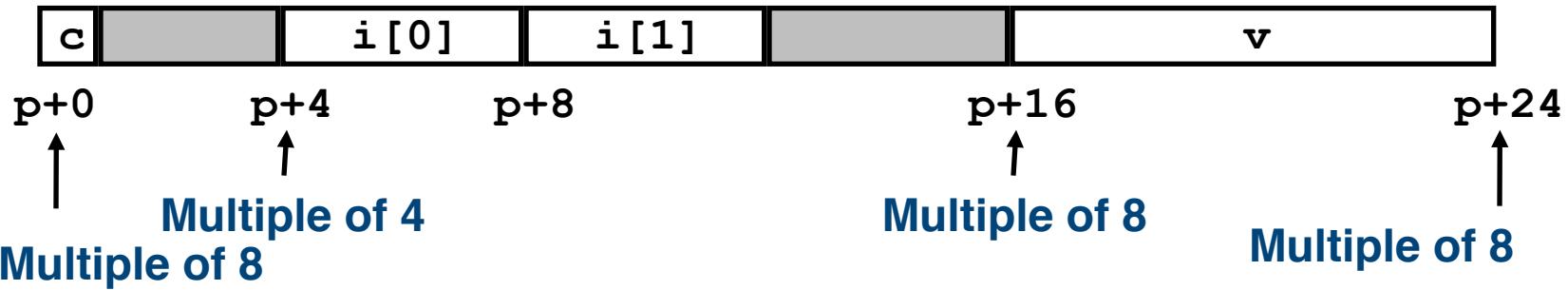
```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *p;
```



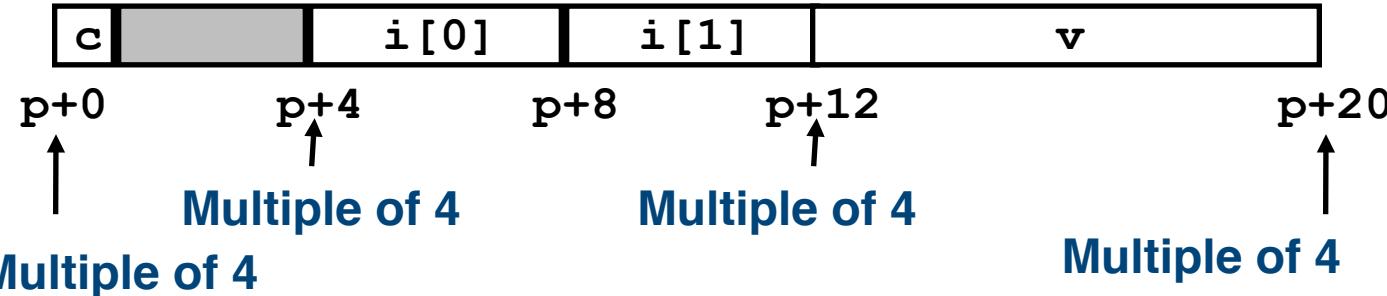
Linux vs. Windows

- Windows (including Cygwin):
 - $K = 8$, due to double element

```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *p;
```



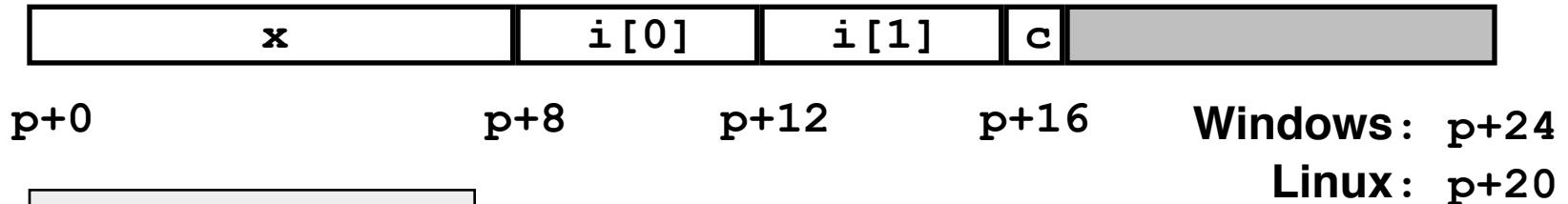
- Linux:
 - $K = 4$; `double` treated like a 4-byte data type



Overall alignment requirement

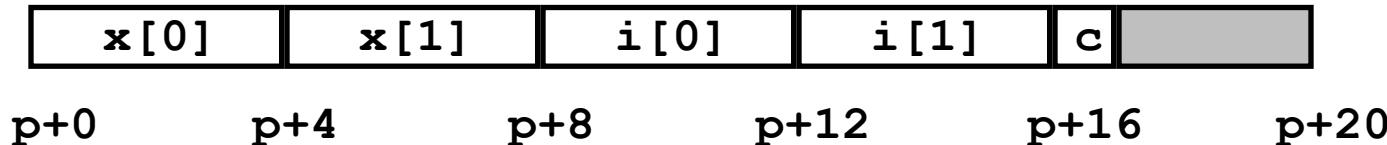
```
struct S2 {  
    double x;  
    int i[2];  
    char c;  
} *p;
```

p must be multiple of:
8 for Windows
4 for Linux



```
struct S3 {  
    float x[2];  
    int i[2];  
    char c;  
} *p;
```

p must be multiple of 4 (in either OS)



Ordering elements within structure

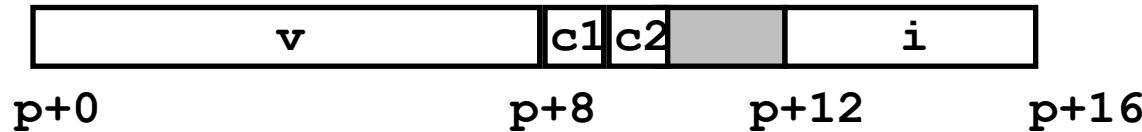
```
struct S4 {  
    char c1;  
    double v;  
    char c2;  
    int i;  
} *p;
```

10 bytes wasted space in Windows



```
struct S5 {  
    double v;  
    char c1;  
    char c2;  
    int i;  
} *p;
```

2 bytes wasted space

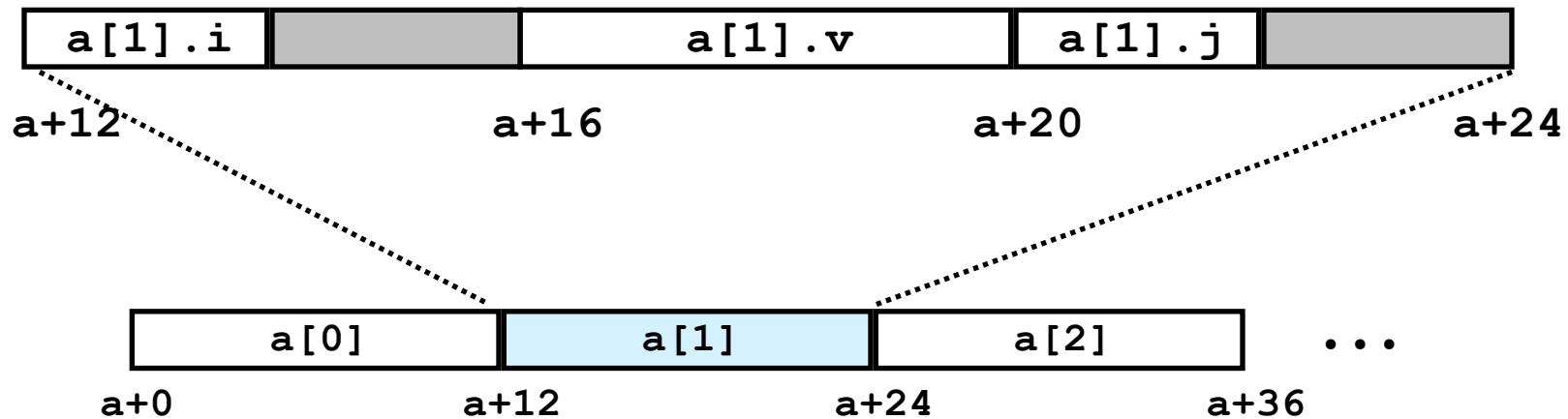


Arrays of structures

- Principle

- Allocated by repeating allocation for array type
- In general, may nest arrays & structures to arbitrary depth

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```



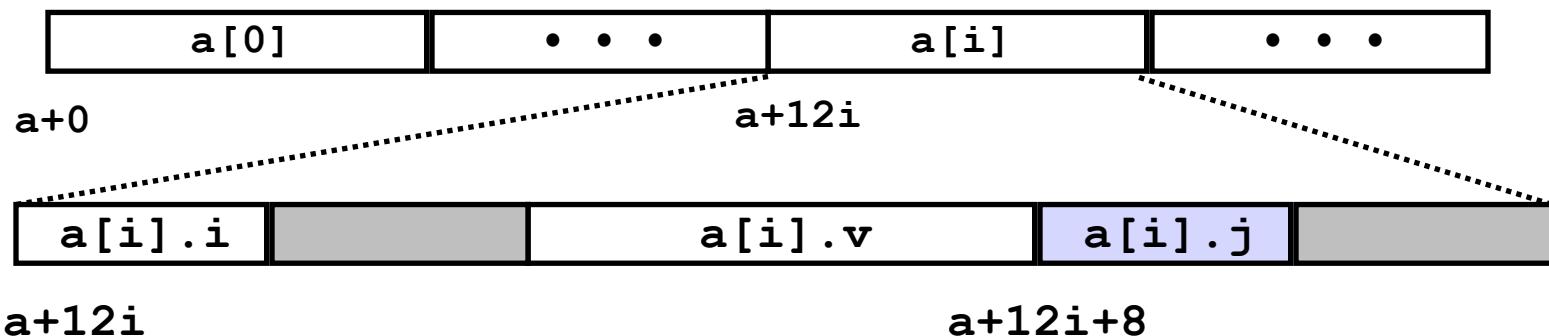
Accessing element within array

- Compute offset to start of structure
 - Compute $12*i$ as $4*(i+2i)$
- Access element according to its offset within structure
 - Offset by 8
 - Assembler gives displacement as $a + 8$
 - Linker must set actual value

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```

```
short get_j(int idx)  
{  
    return a[idx].j;  
}
```

```
# %eax = idx  
leal (%eax,%eax,2),%eax # 3*idx  
movswl a+8(,%eax,4),%eax
```

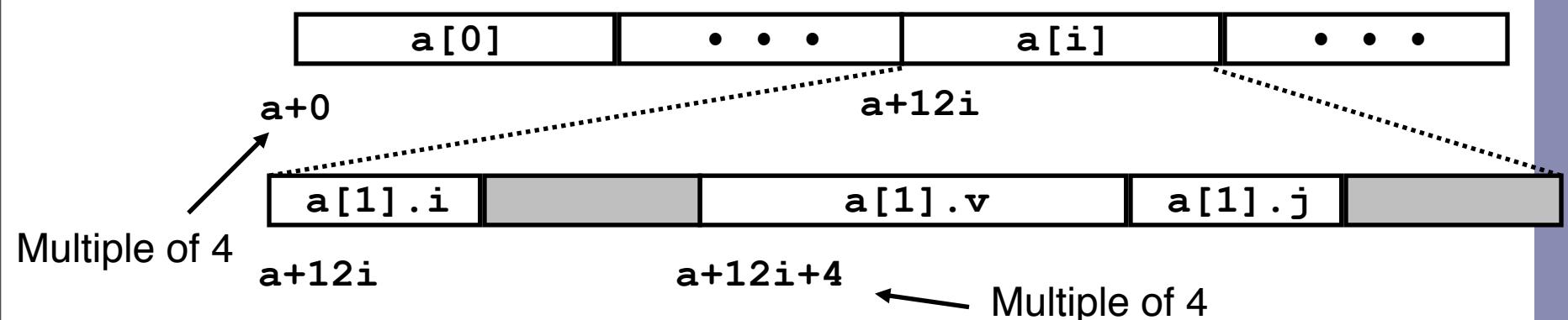


Satisfying alignment within structure

- Achieving Alignment

- Starting address of structure array must be multiple of worst-case alignment for any element
 - i must be multiple of 4
- Offset of element within structure must be multiple of element's alignment requirement
 - v 's offset of 4 is a multiple of 4
- Overall size of structure must be multiple of worst-case alignment for any element
 - Structure padded with unused space to be 12 bytes

```
struct S6 {  
    short i;  
    float v;  
    short j;  
} a[10];
```



Checkpoint

Checkpoint

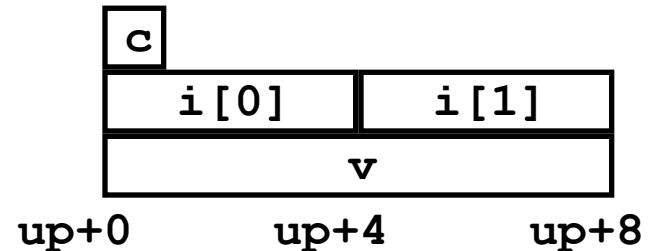


Union allocation

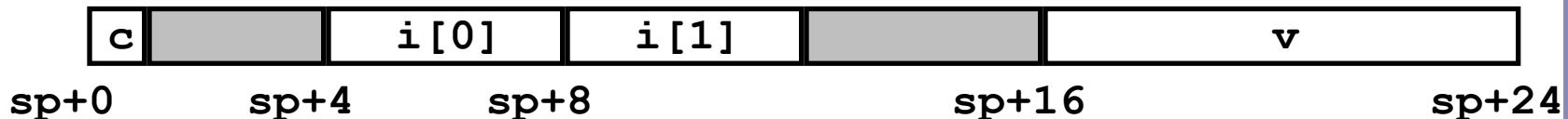
- Principles
 - Overlay union elements
 - Allocate according to largest element
 - Can only use one field at a time

```
struct S1 {  
    char c;  
    int i[2];  
    double v;  
} *sp;
```

```
union U1 {  
    char c;  
    int i[2];  
    double v;  
} *up;
```

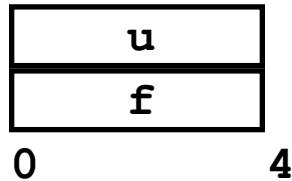


(Windows alignment)



Using union to access bit patterns

```
typedef union {  
    float f;  
    unsigned u;  
} bit_float_t;
```



```
float bit2float(unsigned u) {  
    bit_float_t arg;  
    arg.u = u;  
    return arg.f;  
}
```

```
unsigned float2bit(float f) {  
    bit_float_t arg;  
    arg.f = f;  
    return arg.u;  
}
```

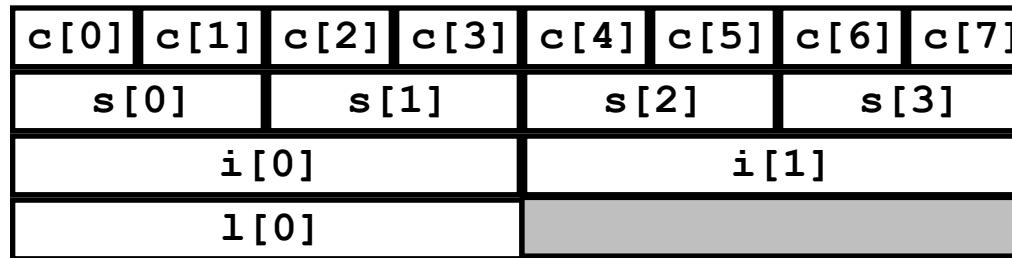
- Get direct access to bit representation of float
- `bit2float` generates float with given bit pattern
 - NOT the same as `(float) u`
- `float2bit` generates bit pattern from float
 - NOT the same as `(unsigned) f`

Byte ordering revisited

- Idea
 - Short/long/quad words stored in memory as 2/4/8 consecutive bytes
 - Which is most (least) significant?
 - Can cause problems when exchanging binary data between machines
- Big Endian
 - Most significant byte has lowest address
 - PowerPC, Sparc
- Little Endian
 - Least significant byte has lowest address
 - Intel x86, Alpha

Byte ordering example

```
union {
    unsigned char c[8];
    unsigned short s[4];
    unsigned int i[2];
    unsigned long l[1];
} dw;
```



Byte ordering example (Cont.).

```
int j;
for (j = 0; j < 8; j++)
dw.c[j] = 0xf0 + j;

printf("Characters 0-7 == [0x%x,0x%x,0x%x,0x
%x,0x%x,0x%x,0x%x,0x%x]\n",
dw.c[0], dw.c[1], dw.c[2], dw.c[3],
dw.c[4], dw.c[5], dw.c[6], dw.c[7]);

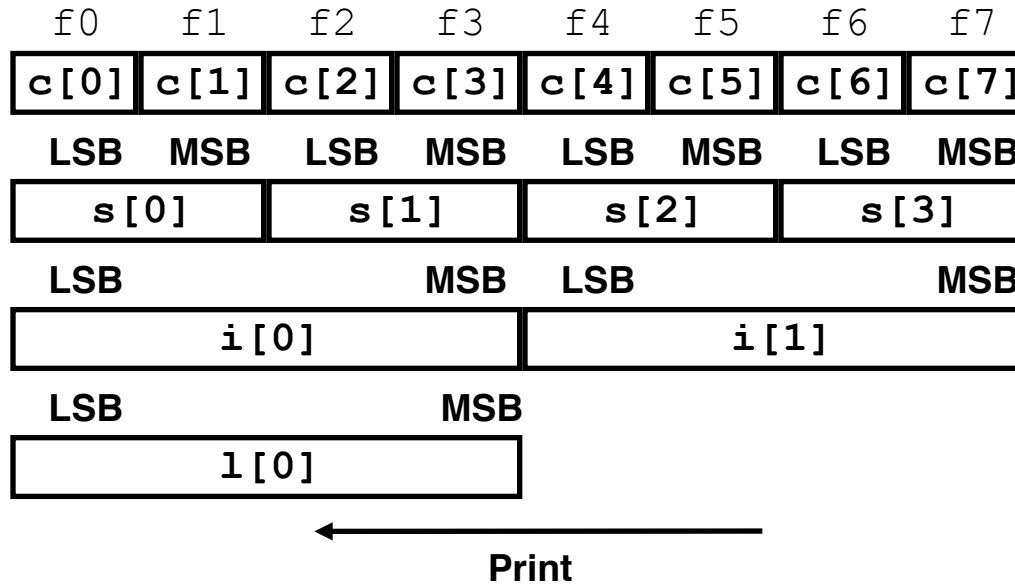
printf("Shorts 0-3 == [0x%x,0x%x,0x%x,0x%x]
\n",
dw.s[0], dw.s[1], dw.s[2], dw.s[3]);

printf("Ints 0-1 == [0x%x,0x%x]\n",
dw.i[0], dw.i[1]);

printf("Long 0 == [0x%lx]\n",
dw.l[0]);
```

Byte ordering on x86

LittleEndian

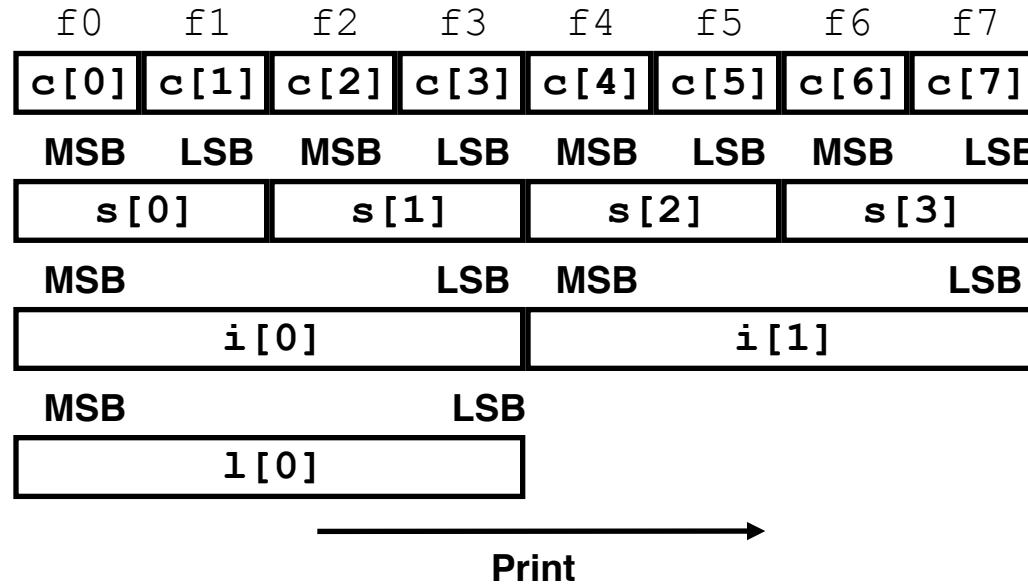


Output on Pentium:

```
Characters 0-7 == [0xf0,0xf1,0xf2,0xf3,0xf4,0xf5,0xf6,0xf7]
Shorts      0-3 == [0xf1f0,0xf3f2,0xf5f4,0xf7f6]
Ints        0-1 == [0xf3f2f1f0,0xf7f6f5f4]
Long         0    == [f3f2f1f0]
```

Byte ordering on sun

BigEndian

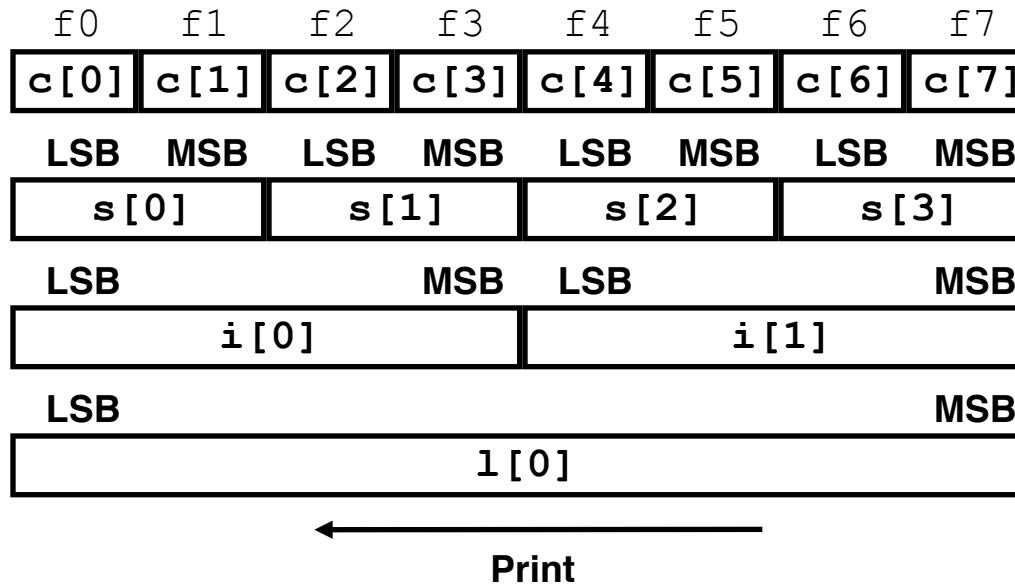


Output on Sun:

```
Characters 0-7 == [0xf0,0xf1,0xf2,0xf3,0xf4,0xf5,0xf6,0xf7]
Shorts      0-3 == [0xf0f1,0xf2f3,0xf4f5,0xf6f7]
Ints       0-1 == [0xf0f1f2f3,0xf4f5f6f7]
Long        0    == [0xf0f1f2f3]
```

Byte ordering on alpha

LittleEndian



Output on Alpha:

Characters	0-7 ==	[0xf0, 0xf1, 0xf2, 0xf3, 0xf4, 0xf5, 0xf6, 0xf7]
Shorts	0-3 ==	[0xf1f0, 0xf3f2, 0xf5f4, 0xf7f6]
Ints	0-1 ==	[0xf3f2f1f0, 0xf7f6f5f4]
Long	0 ==	[0xf7f6f5f4f3f2f1f0]

Summary

- Arrays in C
 - Contiguous allocation of memory
 - Pointer to first element
 - No bounds checking
- Compiler Optimizations
 - Compiler often turns array code into pointer code (`zd2int`)
 - Uses addressing modes to scale array indices
 - Lots of tricks to improve array indexing in loops
- Structures
 - Allocate bytes in order declared
 - Pad in middle and at end to satisfy alignment
- Unions
 - Overlay declarations
 - Way to circumvent type system